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**DIVERSITY IN RETURNS TO EDUCATION IN EUROPE.  
THE EMPIRICAL IMPORTANCE OF THE SYSTEMS  
OF THE REGRESSION APPROACH**

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The aim of the paper is the formal comparison of returns to education for a set of European countries. We apply the system of Seemingly Unrelated Regression Equations (SURE) to obtain the parameters of the Mincerian equations. The differences between the parameters were tested given two alternative stochastic assumptions. In the first model, no contemporaneous correlations between error terms in the system are imposed. In the second approach, the unrestricted covariance matrix is considered, making error terms stochastically dependent. The contemporaneous correlations of error terms in the SURE system were empirically supported. The rich parameterisation of the covariance matrix of contemporaneous relations reduced statistical uncertainty about differences in parameters describing return to education. Therefore, the country heterogeneity of return on education, which seems intuitively correct, was obtained in the system of regressions with a complex stochastic structure.

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## 1. INTRODUCTION

The relationship between earnings and investment in education has been obvious since “The Wealth of Nations” was published in 1776 by Adam Smith. In particular Smith claimed that part of the time spent at the craft by the master together with the apprentice is devoted to training activity rather than production. Thus Smith, formulating the roots of scientific insight into economic processes, highlighted the importance of the investment in on-the-job training.

The issues of human capital have been analysed by many economists despite the serious problems with the formal theoretical framework and the measurement. The pioneer trials of the quantitative assessment of the human

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capital and estimation of the impact on the distribution of wages were performed by Mincer (1958). In this seminal paper the author underlined that human capital itself (as measured by the level of skills and abilities of an individual) is a non-measurable variable. However, he introduced the concept of investments in human capital interpreted as the process of learning and gaining abilities. Mincer identifies two kinds of investments in human capital, namely the investments in formal education (measured by years of schooling completed) and investments during the working life (measured by years of work experience). The contribution of Mincer to the research on human capital is enormous. He analysed both the impact of the individual schooling, as well as the work experience, on the properties of the distribution of earnings. Additionally, wages seem to increase with schooling level, age and occupational hierarchy (see Chiswick and Mincer, 2003, pp. 5-8).

The theoretical background that enables to describe formally the economic impact of human abilities on wages is the Mincer model. It assumes a quadratic dependence between the logarithm of the expected earnings and the given number of years of schooling. According to the Mincer model the earnings of an individual is an increasing function of the level of education, as measured by the years of formal schooling. Also, it is an increasing and concave function of experience, measured simply by the age of the individual. The original version of the Mincer model was subject to many generalisations. According to Lemieux (2006), the most important generalisation concerns the much more complicated nonlinear relationship between the rates of returns from human capital investment and earnings. Despite many generalisations, it seems that the Mincer model is still the basis for the empirical analyses of wage distribution as well as the relation between wages and existing human capital<sup>1</sup>.

One can also point out some disadvantages of the Mincer model. First, the model does not consider other determinants of wages, except for the level of education and work experience. Furthermore, it is possible to educate oneself and work simultaneously. It is worth mentioning that reflecting such a case in economic data is nearly impossible.

Initially Mincer estimated rates of returns from on-the-job training and their impact on the wage distribution for several different occupations. He showed that earnings profiles imply a decline in on-the-job training

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<sup>1</sup> The human capital earnings function has become a technique accepted, for example, by the courts in analyses of earnings. It is used to estimate the value of lost earnings due to injury or death or resulting from discrimination (see Chiswick, 2003, p. 25).

investments with age. Mincer also showed that on-the-job training investments increase with the level of schooling. The Mincer concept prompted new studies, however the necessity of some modification of the model was crucial. For example, the nonlinear relationship between wages and schooling received particular attention; Lemieux, 2006, p. 4, and many others.

Starting from Mincer (1974), the issues of wage and human capital distribution have been studied by many authors. The empirical analyses indicate that the rate of return on education is equal or less than 10% of initial income per additional year of education or 30-35% for achieving a higher level. Several reviews of the empirical results can be found in the literature; see Psacharopoulos (1994), Psacharopoulos and Patrinos (2004), Hanushek and Woessmann (2010), Strauss and de La Maisonnette (2007). Initially, in the problem of the estimation of the return on education, the simple linear regression with OLS estimator has been commonly used; see Becker and Chiswick (1966) and Mincer (1974). In the last decade the quantile regression estimator was also used by, among others, Ning (2010), Newell and Reilly (2001). There are, however, numerous contesting opinions in the literature expressing reservations towards the empirical results based on simple econometric frameworks. The issue of selection problems and heterogeneity in returns was addressed by Carneiro and Heckman (2002) and Blundell, Dearden and Sianesi (2005). Also, the decision made by individuals to take on more education involves many factors like individual ability, family background and preferences, which may be measured imprecisely. The endogeneity and causality problems in labour market studies was addressed by Heckman (1974), Heckman et al. (2006, 2008), Li and Tobias (2011). The impact of these effects on the return on education was discussed by Card (2001). Also, the importance of the observed and unobserved heterogeneity in the estimation of the return on education parameters was analysed by Willis and Rosen (1979). As the heterogeneity seems to be a serious and interesting issue, its analyses were performed according to particular education levels (see Aakvik et al., 2010) as well as different groups (Henderson et al., 2011) and parameters' estimates (Koop, Tobias, 2004).

Parameters of the Mincer regression are estimated using both individual and aggregated data observed for a country by labour force or employers' surveys. On the macro level, Mincerian equations were estimated on the basis of regressions for both cross-section data and time series; see Hausman and Taylor (1981), Moretti (2004), Krueger and Lindahl (2001). The main

assumption for the cross-sectional analysis is the homogeneity of the regression parameters. Consequently, the impact of education and the experience on the observed wages do not vary across countries or across any groups of individuals.

Cross-country regressions were also performed by Hanushek and Zhang (2006), and more recently by Hanushek et al. (2015), Montenegro et al. (2014) and Roszkowska (2014). They reported country heterogeneity of returns to human capital analysing its estimated values varying across countries. The authors applied a multilevel modelling strategy, building regression of resulted returns to skills variability on alternative skill measures (like numeracy, literacy, problem-solving and others). However, a detailed insight into the significance of the observed returns to skill differences is missing. Since the stochastic assumptions imposed in the underlying regression models may be different, the issue of formal statistical testing if observed returns to skill are different, is important.

The main goal of the paper is to estimate Mincerian equation parameters and to formally conclude about the heterogeneity of the return on education effect across European countries. We check if the standard econometric panel regression strategy is correct in the view of the aggregated data. Since the panel data approach relies on the imposed constancy of the return on education effect across the analysed set of countries, we relax this assumption in our research. The variability of parameters describing the impact of years of schooling to the wages, results from the application of the system of Seemingly Unrelated Regression Equations (SURE). Recently this classic yet very promising approach to modelling heterogeneity has received particular attention in cases of convergence analysis or the relationship between credit and growth; see Pipień and Roszkowska (2018) and Olszak and Pipień (2016), respectively.

In this paper the differences between parameters are subject to a testing procedure. In the first model, we assume that there are no contemporaneous correlations between error terms in the system. The second approach assumes the non-zero correlations in the covariance matrix of the error terms. We discuss the results of the testing and provide a classification of a set of European countries with respect to the strength of the return on education effect. Moreover, we indicate plausible reasons for that diversification.

## 2. PARAMETER HETEROGENEITY IN WAGE EQUATION

The basic Mincer wage equation is as follows:

$$\ln wage_t = \alpha_0 + \alpha_1 edu_t + \alpha_2 age_t + \alpha_3 age_t^2 + \varepsilon_t, \quad t=1, \dots, T, \quad (1)$$

where  $\ln wage_t$  is the logarithm of the hourly wage observed in  $t$ -th major occupation group, while  $age_t$  and  $edu_t$  describe age and the average level of education of the group. According to Mincer (1974) and Heckman et al. (2006), when specific measures of post-school investment are unavailable, potential work experience can be approximated simply by age. In Zoghi (2010), Lacuesta et al. (2011), Bolli and Zurlinden (2012), Nilsen et al. (2011), the *age* or *work experience* variables are used only up to the particular age group because observations on the exact number of years corresponding with those variables are not available.

The parameters of interest are  $\alpha_2$  and  $\alpha_3$ , describing the impact of the age to the salary. Parameter  $\alpha_1$  informs us about the strength of the return on education effect. Suppose we observe the aforementioned variables for  $j$ -th country ( $j=1, \dots, n$ ) and we want to formulate the Mincer equation with structural parameters that vary across countries. Let us consider the following system of regressions:

$$\ln wage_{ij} = \alpha_{0j} + \alpha_{1j} edu_{ij} + \alpha_{2j} age_{ij} + \alpha_{3j} age_{ij}^2 + \varepsilon_{ij}, \quad j=1, \dots, n, \quad (2)$$

where  $j$  denotes the number of a country. The error term  $\varepsilon_{ij}$  in (2) captures the impact of effects not involved with the age and the average level of education of the group, to the variability of wage. These effects may concern country specific structural or institutional conditions, cultural differences, the distribution of talents and others. Hence the proper stochastic assumptions in (1) and (2) are crucial when modelling the relationship between wage and the level of education. In the regression (2), having its roots in the Mincer theory, the endogeneity problem can be met, particularly with reference to the education variable. To resolve that problem, estimation techniques utilising instrumental variables (IV approach) can be applied. However, as suggested in Dickson and Harmon (2011) and Heckman and Urzua (2010), IV estimates rest on strong a priori data assumptions and the results may vary with respect to different sets of instruments applied in the estimation.

The standard assumption that, for each  $t$ , Gaussian error terms  $\varepsilon_{ij}$  in (2) are uncorrelated, makes the system of equations independent. This case, denoted by  $M_0$ , formally refers to the standard empirical strategy when country Mincer regressions are estimated separately. However, in general, error terms  $\varepsilon_{ij}$  may exhibit cross correlation and system (2) can be treated as a Seemingly Unrelated Regression Equations (SURE) model. This case we define as  $M_1$ . Nonzero contemporaneous correlations of error terms in (2) define an ampler stochastic structure and enables testing formally  $M_0$  as a special case. Also, the standard interpretation of nonzero contemporaneous correlations is used as indicators describing linkages in the variability of a related variable across countries.

Denote by  $\varepsilon_t = (\varepsilon_{t1}, \dots, \varepsilon_{tn})$  the row vector of error terms at time  $t$  with the covariance matrix  $\Sigma$ . In the case of model  $M_1$  the matrix  $\Sigma$  is symmetric and positive definite with  $n(n+1)/2$  free elements  $\sigma_{ij}^2$ ,  $i=1, \dots, n$  and  $j=1, \dots, n$ . Standard notation gives the variance of the error terms in  $i$ -th country as  $\sigma_{ii}^2 > 0$  and covariance between error terms in  $j$ -th and  $i$ -th country denoted by  $\sigma_{ij}^2$ . The system of equations (2) can be written in the following standard regression form:

$$y^{(j)} = x^{(j)}\alpha^{(j)} + \varepsilon^{(j)}, \quad j=1, \dots, n,$$

where  $y^{(j)} = (y_{1j}, \dots, y_{Tj})'$ ,  $x^{(j)} = (x_{1j}, \dots, x_{Tj})'$ , with  $x_{ij} = (1, edu_{ij}, age_{ij}, age_{ij}^2)$ ,  $\varepsilon^{(j)} = (\varepsilon_{1j}, \dots, \varepsilon_{Tj})'$  and  $\alpha^{(j)} = (\alpha_{0j}, \alpha_{1j}, \alpha_{2j}, \alpha_{3j})'$ . In the next step we stack the observations expressing the system of regression equations in the closed form:

$$Y = X\alpha + \varepsilon, \quad (3)$$

where  $Y_{[nTx1]} = (y^{(1)'}, \dots, y^{(n)'})'$ ,  $\varepsilon_{[nTx1]} = (\varepsilon^{(1)'}, \dots, \varepsilon^{(n)'})'$ ,  $\alpha_{[n4x1]} = (\alpha^{(1)'}, \dots, \alpha^{(n)'})'$ , and:

$$X_{[nTxn4]} = \begin{pmatrix} x^{(1)} & 0_{[Tx4]} & \cdots & 0_{[Tx4]} \\ 0_{[Tx4]} & x^{(2)} & \ddots & \vdots \\ \vdots & \ddots & \ddots & 0_{[Tx4]} \\ 0_{[Tx4]} & \cdots & 0_{[Tx4]} & x^{(n)} \end{pmatrix}.$$

Simple calculations yield the form of covariance matrix for the error term  $\varepsilon$  in (3):

$$V(\varepsilon) = \Sigma \otimes I_n,$$

where  $\otimes$  denotes the Kronecker product. The form of the covariance matrix of  $\varepsilon$  makes system (3) a generalised linear regression. Given  $\Sigma$ , the Aitken Generalised Least Squares estimator of all parameters in the system can be expressed in the following form:

$$\hat{\alpha}_{GLS} = \left( X'(\Sigma \otimes I_n)^{-1} X \right)^{-1} X'(\Sigma \otimes I_n)^{-1} y,$$

with the covariance matrix of the estimator given as follows:

$$V(\hat{\alpha}) = \left( X'(\Sigma \otimes I_n)^{-1} X \right)^{-1}.$$

In the case  $M_0$ , where  $\Sigma = \text{diag}(\sigma_{11}^2, \dots, \sigma_m^2)$ , we have:

$$\hat{\alpha} = \hat{\alpha}_{OLS} = (X'X)^{-1} X'y,$$

which is equivalent to the application of *OLS* estimator for each equation separately. In general case,  $M_1$ , we have to estimate covariance matrix  $\Sigma$ . In the empirical part of the paper we apply the Zellner (1962) method, and estimate elements of matrix  $\Sigma$  based on OLS residuals, denoted by  $\hat{\varepsilon}_{[nTx1]} = (\hat{\varepsilon}^{(1)'}, \dots, \hat{\varepsilon}^{(n)'})'$ . The estimated *GLS*, proposed by Zellner (1962) takes the form:

$$\hat{\alpha}_{EGLS} = \left( X'(S \otimes I_n)^{-1} X \right)^{-1} X'(S \otimes I_n)^{-1} y,$$

with approximated small sample covariance matrix of the estimator:

$$\hat{V}(\hat{\alpha}_{EGLS}) = \left( X'(S \otimes I_n)^{-1} X \right)^{-1},$$

where

$$S = \frac{1}{T} \left( \hat{\varepsilon}^{(1)}, \dots, \hat{\varepsilon}^{(n)} \right)' \left( \hat{\varepsilon}^{(1)}, \dots, \hat{\varepsilon}^{(n)} \right). \quad (4)$$

The empirical importance of the system of regressions is confirmed when matrix  $S$  indicates that  $\Sigma$  is not diagonal. This is clearly implied by possible cross correlations of error terms. Another important issue making the system

analysis possible and nontrivial is the form of the matrix of explanatory variables  $X$ . In the case of a system of regressions (3), the same matrix of explanatory variables is applied in each equation, namely for each  $j = 1, \dots, n$  we have  $x^{(j)} = x$ . Consequently, matrix  $X$  takes the form:

$$X_{[nT \times n4]} = \begin{pmatrix} x & \mathbf{0}_{[Tx4]} & \cdots & \mathbf{0}_{[Tx4]} \\ \mathbf{0}_{[Tx4]} & x & \ddots & \vdots \\ \vdots & \ddots & \ddots & \mathbf{0}_{[Tx4]} \\ \mathbf{0}_{[Tx4]} & \cdots & \mathbf{0}_{[Tx4]} & x \end{pmatrix} = x \otimes I_n.$$

This extremely simplifies the method of estimation since by some basic properties of the Kronecker product we get:

$$\begin{aligned} \hat{\alpha}_{GLS} &= \left( (x \otimes I_n)' (\Sigma \otimes I_n)^{-1} (x \otimes I_n) \right)^{-1} (x \otimes I_n)' (\Sigma \otimes I_n)^{-1} y = \\ &= (X'X)^{-1} X'y = \hat{\alpha}_{OLS} \end{aligned}$$

This result holds irrespective of whether the covariance matrix is diagonal or unrestricted. However, in the analysed case of matrix  $X$ , the difference between estimation with the use of  $\hat{\alpha}_{GLS}$  and  $\hat{\alpha}_{OLS}$  is subtler and concerns the form of the covariance matrices. Since  $\hat{\alpha}_{OLS}$  results from the assumption that matrix  $\Sigma$  is diagonal, the small sample approximation of the covariance matrix of the estimator  $\hat{\alpha}_{OLS}$  is of a similar form as in the case of  $\hat{\alpha}_{OLS}$ , but the diagonal matrix  $S_{diag} = \text{diag}(s_{11}^2, \dots, s_{nn}^2)$  is applied as estimator of  $\Sigma = \text{diag}(\sigma_{11}^2, \dots, \sigma_{nn}^2)$ :

$$\hat{V}(\hat{\alpha}_{OLS}) = \left( X' (S_{diag} \otimes I_n)^{-1} X \right)^{-1},$$

with  $s_{jj}^2 = \frac{1}{T} \hat{\varepsilon}^{(j)'} \hat{\varepsilon}^{(j)}$   $j = 1, \dots, n$ . The diagonal elements of  $\hat{V}(\hat{\alpha}_{OLS})$  and  $\hat{V}(\hat{\alpha}_{EGLS})$  are the same and hence the inference about standard errors of structural parameters is the same. However, matrix  $\hat{V}(\hat{\alpha}_{EGLS})$  is not a block diagonal, and in the case of estimation of functions of interest involving regression parameters from different equations, the inference in the case of *EGLS* may not be equivalent to the *OLS* case.

In the empirical part of the paper we test for the statistical significance of differences between parameters describing return on education, namely  $\alpha_{1j}$  for  $j=1, \dots, n$  across countries; see equation (2). We will perform it according to the standard testing procedure that involves the estimation of a linear combination of structural parameters. Suppose we are interested in a linear combination of structural parameters in (3) of the form  $\gamma = c_{[n4 \times 1]} \cdot \alpha_{[n4 \times 1]} = (c^{(1)'}, \dots, c^{(n)'}) \cdot (\alpha^{(1)'}, \dots, \alpha^{(n)'})'$ . Vector  $c_{[n4 \times 1]}$  contains coefficients of a linear combination and is known. We define the *EGLS* and *OLS* estimator of the function of interest  $\gamma$  as follows:

$$\hat{\gamma}_{OLS} = c \cdot \hat{\alpha}_{OLS}$$

and

$$\hat{\gamma}_{EGLS} = c \cdot \hat{\alpha}_{EGLS}.$$

The small sample approximations of the variance of estimators are given as follows:

$$\hat{V}(\hat{\gamma}_{OLS}) = c \cdot \hat{V}(\hat{\alpha}_{OLS}) \cdot c'$$

and

$$\hat{V}(\hat{\gamma}_{EGLS}) = c \cdot \hat{V}(\hat{\alpha}_{EGLS}) \cdot c'.$$

If the linear combination  $\gamma$  involves parameters from different equations, the variance obtained on the basis of the *OLS* estimator is different from the one obtained according to the *EGLS* procedure. This may cause different results of inference about  $\gamma$ , particularly in cases of testing the significance of some restrictions.

The aforementioned procedure can be applied for system (2) in testing the country heterogeneity of parameters. Suppose we are interested in testing whether the difference between return on education in  $i$ -th country is significantly different from the return on education in  $j$ -th country. More formally we are interested in testing the following hypothesis framework:

$$\begin{aligned} H_0 : \alpha_{1i} - \alpha_{1j} &= 0 \\ H_1 : \alpha_{1i} - \alpha_{1j} &\neq 0. \end{aligned} \tag{5}$$

This can be conducted on the basis of the function  $\gamma^{ij} = c_{[n4 \times 1]} \cdot \alpha_{[n4 \times 1]}$ , with  $c_{[n4 \times 1]} \cdot (c^{(1)'}, \dots, c^{(n)'})$  such that  $c^{(i)} = (0, 1, 0, 0)$ ,  $c^{(j)} = (0, -1, 0, 0)$  and

$c^{(m)} = (0,0,0,0)$  for all remained, namely for  $m \in \{1, \dots, n\} \setminus \{i, j\}$ . In this case, the  $\gamma^{ij}$  simply means difference between  $\alpha_{1,i}$  and  $\alpha_{1,j}$ , and testing country heterogeneity can be equivalently performed on the basis of the following testing hypothesis:

$$H_0 : \gamma^{ij} = 0$$

$$H_1 : \gamma^{ij} \neq 0.$$

The standard procedure of Student's  $t$ -test can be applied, with the test statistics utilising the standard errors defined as square roots of  $\hat{V}(\hat{\gamma}_{EGLS})$  in the case of an *EGLS* estimation procedure or of  $\hat{V}(\hat{\gamma}_{OLS})$  in the case of a simpler method, based on the *OLS* estimator. It is interesting how the form of matrix  $\Sigma$  influences the results of testing the heterogeneity of parameters. In the empirical part of the paper we perform those tests, making comparison of results in both cases of the form of matrix  $\Sigma$ .

### 3. EMPIRICAL ANALYSIS

The empirical analysis presented in the paper is based on the cross-section series taken from the European Union Structure of Earnings Survey (SES), a large representative enterprise sample survey. The SES provides comparable information on the level of remuneration and characteristics of employees such as sex, age and occupation. The analysed dataset contains reliable data on wages and not declared like in the case of data gathered from labour force surveys (LFS). Additionally, LFS may not be representative, because the survey is not obligatory and hence a large refusal rate (sometimes even more than 50%) with regards to the question about the salary may occur. However, as the majority of workers are employed in enterprises with at least ten employees (see Table 4) and the structures of employment across the analysed countries do not differ substantially, we do not expect serious impact of this drawback.

The business activities included in the survey are those from enterprises operating in sections B to S, excluding O, according to NACE Rev. 2; see Table 5 in Appendix for a detailed description. The selection of the sample and conducting the survey is prepared by national statistics offices. The invaluable advantage of the survey is the credibility of data concerned with individuals' wages. Contrary to data from Labour Force Survey (LFS), the data on remuneration concerns the real data coming from employers and not

those declared by respondents. We do not have access to the observed individual wages from the SES and hence in the empirical analysis we consider partially aggregated information, covering average wage corresponding to the particular occupational group and appropriate age group.

The structure and distribution of remunerations can be described by the human capital level. The available dataset contains information about occupation. It can be easily utilised to obtain approximated values of the education level. The occupation (profession) is defined as a set of tasks and duties characterized by their high degree and similarity. The profession needs suitable skills and knowledge. A skill is defined as the ability to carry out the tasks and duties of a given job (see International Standard Classifications: ISCO-08, 2012). According to ISCO-08 we separate four major levels of skills. Skill levels are defined by considering the level of education and qualifications gained by on-the-job training or practice. The key factor for the classification of professions is the level of required qualifications rather than the way of achieving them. According to ISCO-08 methodology, there are four levels of skills (see Table 1). The first level requires elementary qualifications and primary or the first stage of basic education. The second level involves individuals with secondary levels of education (basic vocational, general and vocational comprehensive) and post or non-tertiary levels. The third level is related to education accomplished in the first stage tertiary education. The fourth level covers individuals with tertiary level of education.

Table 2 presents the basic descriptive statistics of wages in selected EU countries in 2010. The highest average hourly remunerations (ca. 18-19 PPS) can be observed in Denmark, Ireland and Belgium. The lowest (almost three times lower) are reported in Bulgaria, Romania and Latvia. In the old EU15 countries (except for Portugal), wages were higher than the average of the sample. The similar pattern can be found when studying the diversity of wages. Country statistics show the highest variation of wages in southern European countries (Portugal, Italy, Romania, Bulgaria and Slovenia). The lowest coefficients of variation (below 0.3) were discovered in Denmark and Sweden.

Analysis of wages by skill level (Table 6 in Appendix) shows that the lowest and the least diversified are the earnings in the group with a primary level of education. Higher and more diversified wages can be determined in the group of better qualified workers. The group of those with tertiary education is the most heterogeneous. This set includes, among others, executive professionals, legislators, teachers, medical doctors and artists.

The group of employees with a secondary level of education is also moderately heterogeneous. This group includes clerical support workers, sales workers and machine operators. The study of wages by age in the set of analysed countries (Table 7) indicates the relatively moderate diversification (coefficient of variation equals from 0.3 to 0.4) in the first two age intervals (namely less than 30 years and from 30 to 39 years). Higher wages and higher variation ( $cv = 0.5$ ) appear in the group of employees aged 40.

The preliminary, qualitative analyses (see Tables 2, 6 and 7) indicate that the existing diversification of wages in Europe with respect to the level of skills and labour market experience is strong. Also, higher wages are observed together with a higher level of human capital accumulated by individuals. Our research strategy considers those empirical effects. Consequently, we estimate the total impact of changes in human capital on the wage level in European countries.

The parameters of regression equation (2) were subject to estimation. We assume that  $edu_{ij}$  is the mean skill level according to ISCO-08 of the employee in  $t$ -th major occupation group in country  $j$ ;  $age_{ij}$  – work experience measured by age interval of the employee in  $t$ -th major occupation group in country  $j$  (there are five intervals for age: 2 – less than 30 years, 3 – from 30 to 39 years, 4 – from 40 to 49 years, 5 – from 50 to 59 years, 6 – 60 years or over);  $\alpha_{0j}$  – intercept for country  $j$ ;  $\alpha_{1j}$  – shows the relative change of worker's salary caused by skills' level increase;  $\alpha_{2j}$ ,  $\alpha_{3j}$  – show the impact of work experience on wages. The parameters of the above equation were estimated OLS using cross-section data (64 observations for every country) concerning men and women in 2010 in 22 EU countries<sup>2</sup>.

The results of the estimation are presented in Table 3 and estimated returns on education in Figure 1. In Table 3 we put the point estimates, standard errors (in italics) and  $p$ -values for the zero restriction test of a particular parameter (in square brackets). There is a positive and statistically significant impact of skill level on remuneration. Depending on the country of region, the improvement of skill level resulted in a 17-46% change of salaries. The estimated value of  $\alpha_{1j}$  parameter can be treated as a measure of returns to education in  $j$ -th country. As was mentioned above, the skill level can be easily mapped to education level.

The results in Table 3 demonstrate that the highest returns to education were in NMS countries and Portugal. These economies are characterized by

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<sup>2</sup> From the whole sample of EU countries, the following had to be removed due to missing data: Luxembourg, Lithuania, Croatia, Cyprus and Malta.

relatively low wages and high dispersion of wages (see Table 2). Moreover, the labour force in these countries is characterized by relatively worse educational attainment in tertiary degree and lower labour productivity as compared to other countries (Figures 2 and 3). Additionally, total public expenditures on education (as % of GDP) are lower in these countries (Figure 7). The labour force participation in NMS countries and Portugal also seems lower than in the core EU15 (Figure 4). The obtained results for the 22 European countries converged on the increasing returns to education in selected emerging economies outcomes (see München et al., 2005; Vujčić, Šošić, 2009; Li et al., 2013; Bargain et al., 2009).

The lowest rates of return to education (17-19%) can be found in Denmark and Sweden. Relatively low rates (under 30%) are in the Netherlands, Finland, Ireland, Belgium and France. The labour force in this group of countries is well educated, expenditures on education are relatively substantial and the wages are relatively high and less diversified. In most of the analysed countries the work experience plays a significant role in wage formation. We consider nonlinear dependency between wages and work experience (resulting from the extended Mincer equation). In general, the level of wages can be described by the quadratic function of individuals' work seniority. Each additional year of work experience relates to an increase in the wage, however this effect stays true until the maximum level of remuneration is reached. Then the average wage ceases rising. The differences in returns to work experience are also diversified among countries. Although direct economic interpretation of estimated  $\alpha_2$  parameter as return to work experience is not allowed due to nonlinearities, we can see that the distribution of these estimates is like that for  $\alpha_{1j}$  values. The lowest values are in NMS countries and the highest in the core EU15.

The system of regressions (2) enables us to formally test differences in parameters across countries. In particular, we are interested in testing whether the parameters describing return on education ( $\alpha_{1j}$ ), are heterogeneous across countries. Those parameters were individually statistically significant, however a detailed insight into its heterogeneity across countries is subject to analysis. We perform a series of tests of the form (5) in pairs given two alternative assumptions imposed on the distribution of the error terms. The results of the tests are compared when a diagonal matrix with different variances attached to error terms for a particular country is considered, and alternatively, when the covariance matrix  $\Sigma$  is unrestricted. In both cases, the point estimates of parameters, as well as its individual standard errors are the same in the case of OLS and

Zellner estimator, however the inference about functions of interests involving parameters from different equations may be different due to the highly non-zero estimates of the off-diagonal elements of  $\Sigma$ ; see Table 8.

In the analysed framework *ML* estimates are equivalent for the OLS procedure in model  $M_0$  and the Zellner method in model  $M_1$ . Hence to compare the explanatory power of competing specifications we put in Table 3 the likelihood values at *ML* estimates, together with model information criteria (AIC and BIC). It is clear that model  $M_1$  receives decisive data support compared to model  $M_0$  as the value of the log-likelihood reaches value 1889.709 against value 543.590 attached to the *ML* estimates in model  $M_0$ . We performed a likelihood ratio test of the model  $M_0$  in the null hypothesis obtained as a result of imposing appropriate zero restrictions of matrix  $\Sigma$  in  $M_1$ . The resulted p-value obtained for  $\Sigma$  distribution with 231 degrees of freedom<sup>3</sup> is less than  $10^{-8}$ . This clearly indicates the empirical importance of the general mode framework  $M_1$ . The information criteria AIC and BIC also confirm empirical support in favour of model  $M_1$  in spite of the number of free elements in the unconstrained case of matrix  $\Sigma$ .

The main results of the testing procedures are presented in Figures 5 and 6. We depict the groups of countries with similar, statistically indistinguishable return on education effect. In cases of countries with the same shading there was no data evidence against the zero hypothesis in (5) at 5% significance level. The results presented on Figure 5 were obtained in cases of diagonal covariance matrix  $\Sigma$ , while Figure 6 is related to the unrestricted case. In the case of diagonal covariance matrix, the results of country heterogeneity of return on education are vague and are attributed with great uncertainty. Consequently we identify only two groups of countries with the same effect. The first group consists of Denmark and Sweden, while in the second group the rest of the countries are included. The statistical uncertainty about the differences between the parameters describing return on education in a particular country is substantial. Hence, given the simple stochastic structure of the model, it is impossible to categorize countries in a nontrivial way.

In more complex stochastic assumptions, with unrestricted covariance matrix  $\Sigma$  (see Figure 6), we can distinguish five groups of countries with a statistically similar return on education parameter. In the first group, with the lowest return on education, we still have Denmark and Sweden, but the rest of the countries are split into four groups, separable from the statistical point

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<sup>3</sup>  $[n \times n]$  covariance matrix  $\Sigma$  can be restricted to diagonal case by imposing  $0.5n(n+1)-n$  restrictions.

of view. The Netherlands, Finland, Ireland, Belgium and France are in the second group, while Spain, Latvia, Austria, Germany, Italy, the United Kingdom, Slovakia, the Czech Republic and Estonia constitute the third group. Hungary, Poland, Slovenia and Bulgaria constitute the fourth group, and Romania and Portugal the last group, representing countries with the highest return to education.

## CONCLUSIONS

The main goal of the paper was to estimate the Mincer equation across European countries. The variability of parameters describing the impact of years of schooling (both formal at school and informal in workplace) to wages, was obtained by the application of a system of seemingly unrelated regression equations. We tested formally the differences between the parameters describing returns to formal education. In the first step, no contemporaneous correlations between error terms in the system are imposed, while in the second approach the unrestricted covariance matrix is considered.

Preliminary analysis showed the statistical significance of skills' level impact on wage level in the analysed set of countries. The value of estimated returns to education rate vary from 17% in Scandinavian countries to 40% and more in Southern Europe countries.

In general, countries with low estimated returns to education can be characterized by higher labour force participation rates, better educated population, higher public expenditures on education and lower dispersion of wages. Moreover, in this group of countries, work experience seems to be much more valuable compared to the remaining countries.

The conducted analyses indicate serious concerns about the stochastic structure imposed in a system of regressions applied for country comparisons. The estimates of parameters of equations, describing return on education effect, vary across countries. However, for predominant cases its differences are not statistically significant when simple stochastic assumptions, imposing no correlations between countries, are considered. The contemporaneous correlations of error terms in the SURE system are empirically supported. Also, the rich parameterisation of the covariance matrix of contemporaneous relations reduced statistical uncertainty. Hence, the inferences about return on education effect in a set of countries become more diverse. In the case of the independent regressions, the results of tests about the differences between parameters describing return to education

effect, is unclear and produces great uncertainty. Given the more complex stochastic structure of dependence between error terms it was possible to classify a set of countries in a nontrivial way. The testing procedures distinguish five separable groups of countries with different return on education effect. Hence, the linkages between countries, expressed in the model by contemporaneous correlations of the error term, is empirically important and provide much more interesting results about functions of interest, making the statistical inference about regression parameters unchanged. Consequently, testing the heterogeneity of parameters in the Mincer regressions is not an easy task and can be performed in the system regression approach with more complicated stochastic assumptions.

The obtained regional differences in rates of return to education as a result of complex stochastic assumptions indicate that the returns to education are higher in the CEE than in the EU15 countries. At any reasonable level of significance we can reject the hypothesis of equality returns to education in these analysed countries. However, the standard assumptions about the stochastic structure (panel OLS estimator) indicate equal returns to education in almost all the countries (except Denmark and Sweden). Thus more rigorous assumptions do allow to conclude that the rates of return to education are the same in emerging and developed countries.

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## APPENDIX

Table 1  
ISCO-08 groups and skill levels

ISCO-08 major groups	Skill Level
1 Managers	3 + 4
2 Professionals	4
3 Technicians and Associate Professionals	3
4 Clerical Support Workers	2
5 Service and Sales Workers	2
6 Skilled Agricultural, Forestry and Fishery Workers	2
7 Craft and Related Trades Workers	2
8 Plant and Machine Operators and Assemblers	2
9 Elementary Occupations	1
10 Armed Forces Occupation	1 + 2 + 4

Source: International Standard Classifications: ISCO-08, International Labour Office, Geneva: ILO, 2012, vol. 1.

Table 2  
Descriptive statistics of hourly wages in selected EU countries in 2010 (in PPS)

Country	Mean	Minimum	Maximum	Variance	Coefficient of variation
Austria	16.196	7.330	46.400	64.591	0.4962
Belgium	18.741	10.010	42.140	58.243	0.4072
Bulgaria	5.349	2.340	13.050	7.771	0.5212
Czech Republic	8.060	3.700	20.060	14.024	0.4646
Denmark	19.528	11.750	35.650	29.825	0.2797
Estonia	7.552	3.160	17.840	11.965	0.4580
Finland	16.068	8.990	35.360	38.538	0.3863
France	15.106	8.080	40.320	43.449	0.4364
Germany	17.764	7.520	40.000	67.286	0.4618
Hungary	8.055	3.760	19.730	15.993	0.4965
Ireland	19.313	10.180	40.300	58.440	0.3958
Italy	16.040	7.690	42.550	80.968	0.5610
Latvia	6.238	3.160	13.160	5.978	0.3920
Netherlands	16.471	7.230	32.420	34.222	0.3552
Poland	8.821	4.080	22.620	20.516	0.5135
Portugal	11.422	4.150	31.150	54.673	0.6474
Romania	5.903	2.450	15.250	12.481	0.5985
Slovakia	7.703	3.790	18.970	13.479	0.4766
Slovenia	12.708	5.760	33.910	48.510	0.5481
Spain	14.489	7.390	35.940	44.362	0.4597
Sweden	14.651	9.550	28.050	18.079	0.2902
United Kingdom	16.368	7.590	36.390	53.933	0.4487

Source: authors' own.

Table 3

The results of estimation of parameters in Mincer equations in a set of countries and model selection criteria. We put the point estimates, standard errors (in italics) and p-values for zero restriction test of a particular parameter (in square brackets)

<b>Country</b>	$\alpha_{0i}$	$\alpha_{1i}$	$\alpha_{2i}$	$\alpha_{3i}$
1	2	3	4	5
Austria	0.804517	0.331677	0.426552	-0.03883
	<i>0.218682</i>	<i>0.021472</i>	<i>0.113136</i>	<i>0.01396</i>
	[0.000244]	[1.32E-49]	[0.00017]	[0.005487]
Belgium	1.297771	0.285186	0.335843	-0.02938
	<i>0.142724</i>	<i>0.014014</i>	<i>0.073839</i>	<i>0.009111</i>
	[3.45E-19]	[2.72E-80]	[5.9E-06]	[0.001291]
Bulgaria	0.322091	0.416255	0.113577	-0.01772
	<i>0.228792</i>	<i>0.022465</i>	<i>0.118367</i>	<i>0.014605</i>
	[0.15943]	[2.6E-68]	[0.337467]	[0.22534]
Czech Republic	0.520228	0.346856	0.289626	-0.03328
	<i>0.229066</i>	<i>0.022491</i>	<i>0.118508</i>	<i>0.014622</i>
	[0.023302]	[1.83E-49]	[0.014658]	[0.022989]
Denmark	1.545782	0.174215	0.437635	-0.04545
	<i>0.140934</i>	<i>0.013838</i>	<i>0.072913</i>	<i>0.008997</i>
	[7.53E-27]	[2.09E-34]	[2.51E-09]	[5E-07]
Estonia	0.737041	0.352713	0.205628	-0.03139
	<i>0.238293</i>	<i>0.023397</i>	<i>0.123282</i>	<i>0.015211</i>
	[0.002023]	[1.68E-47]	[0.095563]	[0.039248]
Finland	1.352042	0.258832	0.319167	-0.03292
	<i>0.177835</i>	<i>0.017461</i>	<i>0.092004</i>	<i>0.011352</i>
	[5.48E-14]	[4.25E-46]	[0.000539]	[0.003792]
France	1.259472	0.292803	0.224716	-0.01589
	<i>0.159000</i>	<i>0.015612</i>	<i>0.08226</i>	<i>0.01015</i>
	[4.96E-15]	[9.19E-70]	[0.006383]	[0.117705]
Germany	0.694024	0.339402	0.54815	-0.05546
	<i>0.180304</i>	<i>0.017704</i>	<i>0.093281</i>	<i>0.01151</i>
	[0.000124]	[1.83E-72]	[5.31E-09]	[1.62E-06]
Hungary	0.770683	0.375923	0.068702	-0.0028
	<i>0.204335</i>	<i>0.020063</i>	<i>0.105714</i>	<i>0.013044</i>
	[0.000169]	[1.2E-69]	[0.515876]	[0.830031]

1	2	3	4	5
Ireland	0.992552 <i>0.171045</i> [8.15E-09]	0.26368 <i>0.016794</i> [4.63E-51]	0.571297 <i>0.088491</i> [1.51E-10]	-0.05996 <i>0.010919</i> [4.78E-08]
Italy	0.652806 <i>0.227626</i> [0.004198]	0.340295 <i>0.02235</i> [2.38E-48]	0.448101 <i>0.117763</i> [0.000148]	-0.03797 <i>0.014531</i> [0.009065]
Latvia	0.856984 <i>0.182072</i> [2.78E-06]	0.320107 <i>0.017877</i> [2.34E-64]	0.07136 <i>0.094196</i> [0.448842]	-0.01262 <i>0.011623</i> [0.277664]
Netherlands	0.851423 <i>0.136289</i> [5.63E-10]	0.248588 <i>0.013382</i> [1.3E-68]	0.571987 <i>0.07051</i> [1.13E-15]	-0.05838 <i>0.0087</i> [2.88E-11]
Poland	0.395191 <i>0.227625</i> [0.08277]	0.383528 <i>0.02235</i> [9.74E-60]	0.325102 <i>0.117763</i> [0.005849]	-0.0356 <i>0.01453</i> [0.014422]
Portugal	-0.04775 <i>0.262584</i> [0.855722]	0.46068 <i>0.025783</i> [4.04E-64]	0.463982 <i>0.135849</i> [0.000656]	-0.04216 <i>0.016762</i> [0.012023]
Romania	0.128356 <i>0.269076</i> [0.633422]	0.453002 <i>0.02642</i> [1.18E-59]	0.158483 <i>0.139208</i> [0.255132]	-0.01838 <i>0.017177</i> [0.284655]
Slovakia	0.628832 <i>0.238073</i> [0.008355]	0.341852 <i>0.023376</i> [5.33E-45]	0.223241 <i>0.123168</i> [0.070137]	-0.02638 <i>0.015197</i> [0.082884]
Slovenia	0.764813 <i>0.190327</i> [6.19E-05]	0.385382 <i>0.018688</i> [3.94E-82]	0.233162 <i>0.098467</i> [0.018031]	-0.01591 <i>0.01215</i> [0.190602]
Spain	1.181748 <i>0.187973</i> [4.4E-10]	0.317969 <i>0.018457</i> [3.75E-60]	0.161371 <i>0.097249</i> [0.09728]	-0.0043 <i>0.011999</i> [0.720075]
Sweden	1.471135 <i>0.14431</i> [1.53E-23]	0.19044 <i>0.014169</i> [1.09E-38]	0.324012 <i>0.07466</i> [1.53E-05]	-0.03441 <i>0.009212</i> [0.000196]
United Kingdom	0.750457 <i>0.186361</i> [5.97E-05]	0.34039 <i>0.018298</i> [8.86E-69]	0.540786 <i>0.096415</i> [2.48E-08]	-0.06146 <i>0.011896</i> [2.76E-07]
Criteria for model selection				
	Model $M_0$		Model $M_1$	
Log-likelihood	543.590		1889.709	
AIC	-289.689		-1307.193	
BIC	-867.181		-3097.418	

Source: authors' own.



Figure 1. Return to education in 2010 (in pp.)

Source: authors' own.

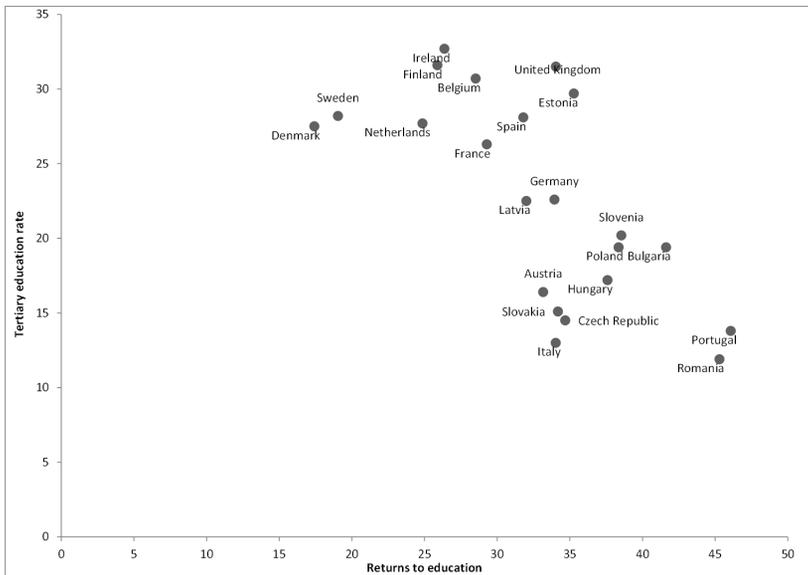


Figure 2. Returns to education vs tertiary education rate (in pp.)

Source: authors' own.

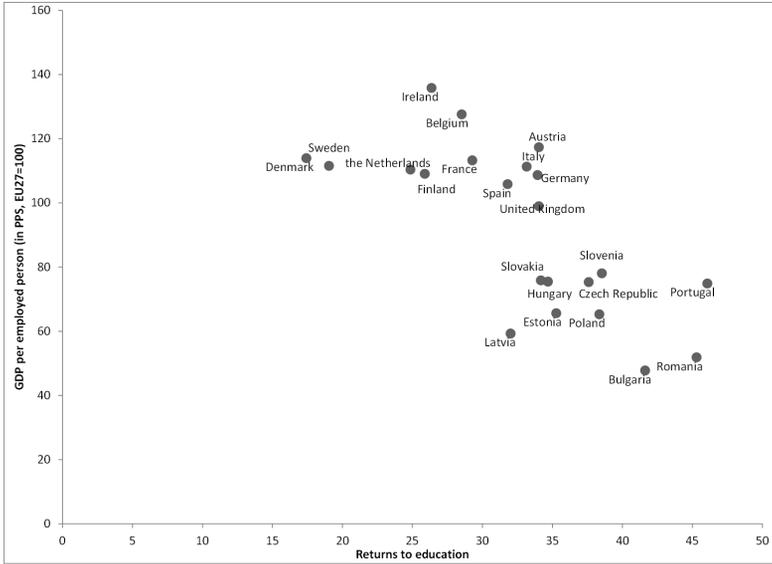


Figure 3. Returns to education vs labour productivity

Source: authors' own.

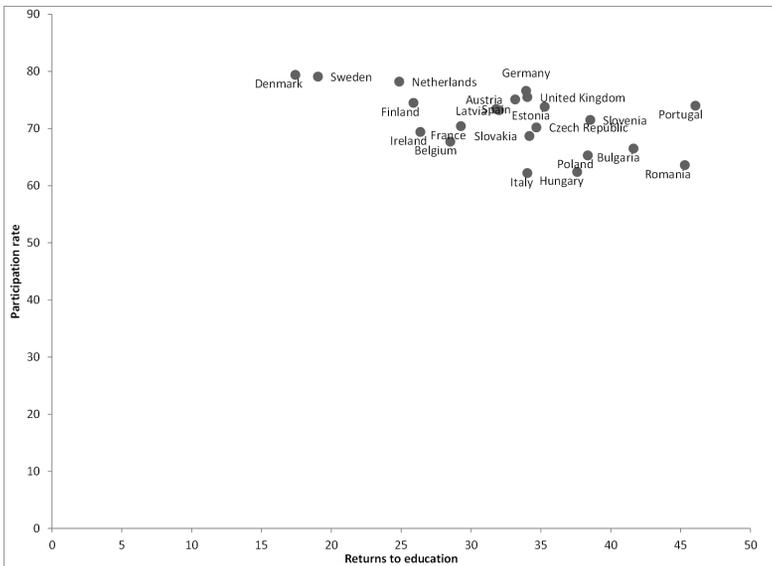


Figure 4. Returns to education vs participation rate

Source: authors' own.



Figure 5. Groups of countries with the same returns to education rates, the case of block-diagonal variance-covariance matrix ( $M_0$ )

Source: authors' own.

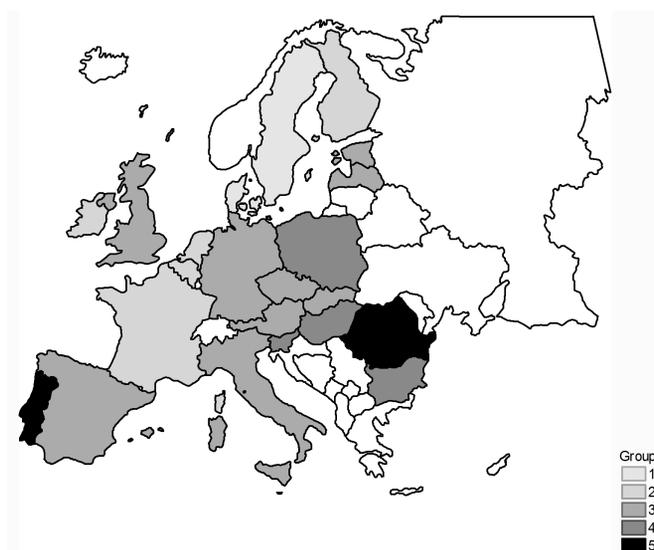


Figure 6. Groups of countries with the same returns to education rates, the case of unrestricted covariance matrix ( $M_1$ )

Source: authors' own.

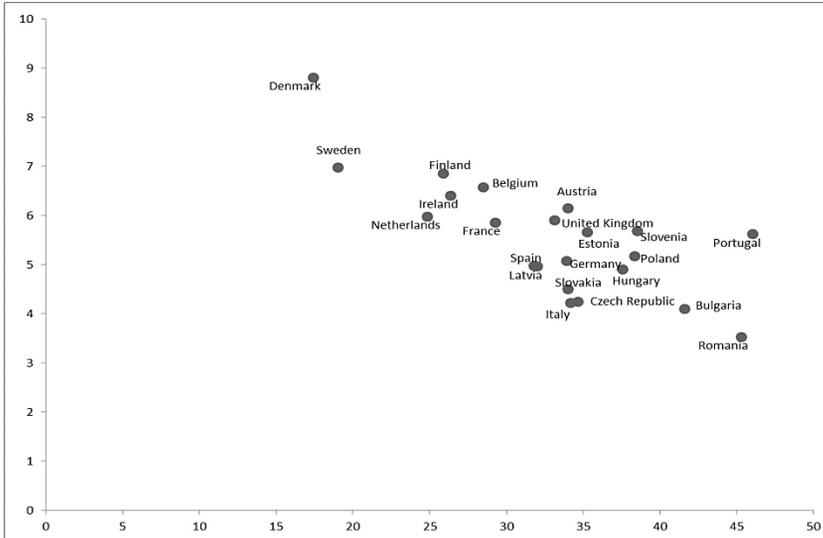


Figure 7. Returns to education vs total public expenditure on education as % of GDP

Source: authors' own.

Table 4

Structure of employees in the population of active enterprises in 2010

Country	Number of employees			Percentage shares of employees		
	From 1 to 4 employees	From 5 to 9 employees	10 employees or more	From 1 to 4 employees	From 5 to 9 employees	10 employees or more
1	2	3	4	5	6	7
Austria	315365	274517	2391849	10.577	9.207	80.217
Belgium	241786	197683	2219584	9.093	7.434	83.473
Bulgaria	267785	183967	1681362	12.554	8.624	78.822
Czech Republic	321417	272505	2957038	9.052	7.674	83.274
Denmark	na	na	na	na	na	na
Estonia	54061	42217	297586	13.726	10.719	75.556
Finland	150630	124031	1144319	10.615	8.741	80.644
France	1513583	1404084	12060243	10.105	9.374	80.520
Germany	2172468	1932273	21610143	8.448	7.514	84.037
Hungary	452300	220710	1626316	19.671	9.599	70.730
Ireland	na	na	na	na	na	na
Italy	1912983	1386445	8470911	16.253	11.779	71.968
Latvia	80696	65848	450843	13.508	11.023	75.469
Netherlands	407213	384481	6466974	5.610	5.297	89.093
Poland	na	na	na	na	na	na
Portugal	498132	376965	2178399	16.313	12.345	71.341

1	2	3	4	5	6	7
Romania	506532	347287	2976298	13.225	9.067	77.708
Slovakia	145215	58634	1150572	10.722	4.329	84.949
Slovenia	91300	51853	453568	15.300	8.690	76.010
Spain	2118670	1327490	8014381	18.487	11.583	69.930
Sweden	308706	233440	1989272	12.195	9.222	78.583
United Kingdom	2546896	1567057	17272274	11.909	7.327	80.764

Note: Number of employees is defined as those persons who work for an employer and who have a contract of employment and receive compensation in the form of wages, salaries, fees, gratuities, piecework pay or remuneration in kind. A worker from an employment agency is considered to be an employee of that temporary employment agency and not of the unit (customer) in which she/he works; na – not available; data covers industry, construction and services except insurance activities of holding companies.

Source: Eurostat.

Table 5

Statistical classification of economic activities in the European Community (NACE)

<b>NACE Rev. 2 Code</b>	<b>Economic activity</b>
A	Agriculture, forestry and fishing
B	Mining and quarrying
C	Manufacturing
D	Electricity, gas, steam and air conditioning supply
E	Water supply; sewerage, waste management and remediation activities
F	Construction
G	Wholesale and retail trade; repair of motor vehicles and motorcycles
H	Transportation and storage
I	Accommodation and food service activities
J	Information and communication
K	Financial and insurance activities
L	Real estate activities
M	Professional, scientific and technical activities
N	Administrative and support service activities
O	Public administration and defence; compulsory social security
P	Education
Q	Human health and social work activities
R	Arts, entertainment and recreation
S	Other service activities
T	Activities of households as employers; undifferentiated goods- and services-producing activities of households for own use
U	Activities of extraterritorial organisations and bodies

Source: [http://ec.europa.eu/eurostat/ramon/nomenclatures/index.cfm?TargetUrl=ACT\\_OTH\\_DFLT\\_LAYOUT&StrNom=NACE\\_REV2&StrLanguageCode=EN](http://ec.europa.eu/eurostat/ramon/nomenclatures/index.cfm?TargetUrl=ACT_OTH_DFLT_LAYOUT&StrNom=NACE_REV2&StrLanguageCode=EN)

Table 6

Mean and coefficient of variation of hourly wages in selected EU countries in 2010 (in PPS) by level of skills

Country	Skill level =1, n=10		Skill level =2, n=24		Skill level =3, n=10		Skill level =4, n=20	
	mean	cv	mean	cv	mean	cv	mean	cv
Austria	8.928	0.123	11.953	0.241	16.774	0.237	24.633	0.341
Belgium	11.786	0.110	14.340	0.138	18.661	0.190	27.539	0.257
Bulgaria	2.650	0.055	3.459	0.193	5.890	0.139	8.695	0.247
Czech Republic	4.359	0.119	5.856	0.205	8.701	0.144	12.235	0.283
Denmark	14.862	0.097	16.674	0.131	20.476	0.177	24.814	0.236
Estonia	4.268	0.199	5.385	0.243	7.961	0.179	11.591	0.235
Finland	10.864	0.127	12.487	0.100	15.649	0.134	23.178	0.270
France	9.400	0.080	11.258	0.100	15.239	0.157	22.509	0.301
Germany	9.592	0.127	13.063	0.187	19.445	0.267	26.651	0.278
Hungary	4.119	0.083	5.720	0.162	7.873	0.114	12.916	0.264
Ireland	12.766	0.142	14.902	0.161	19.966	0.194	27.554	0.279
Italy	8.908	0.101	11.224	0.184	15.504	0.209	25.653	0.398
Latvia	3.620	0.129	4.672	0.171	6.800	0.150	9.147	0.179
Netherlands	10.487	0.173	13.525	0.171	17.597	0.181	22.437	0.255
Poland	4.820	0.132	5.964	0.194	8.378	0.149	14.472	0.249
Portugal	5.004	0.109	7.015	0.263	11.387	0.173	19.937	0.364
Romania	2.614	0.043	3.808	0.243	5.638	0.119	10.196	0.302
Slovakia	4.350	0.109	5.433	0.176	8.444	0.139	11.734	0.307
Slovenia	6.577	0.075	8.579	0.153	12.326	0.163	20.921	0.318
Spain	8.561	0.146	10.689	0.291	14.933	0.264	21.790	0.269
Sweden	10.824	0.077	12.299	0.063	15.319	0.139	19.052	0.243
UK	9.184	0.133	11.998	0.200	16.719	0.202	25.030	0.238

Note: Skill level: 1 - elementary qualifications and primary or the first stage of basic education, 2 –secondary levels of education (basic vocational, general and vocational comprehensive) and post- or non-tertiary levels, 3 –first stage tertiary education, 4 –tertiary level of education; n – no. of observations; mean – average wage in the group; cv – coefficient of variation.

Source: authors' own.

Table 7

Mean and coefficient of variation of hourly wages in selected EU countries in 2010 (in PPS) by age

Country	Age=2, n=12		Age=3, n=14		Age=4, n=14		Age=5, n=12		Age=6, n=12	
	mean	cv								
Austria	11.143	0.280	14.379	0.347	16.664	0.435	18.835	0.458	20.185	0.580
Belgium	13.983	0.242	16.811	0.327	19.209	0.377	21.859	0.405	22.084	0.438
Bulgaria	5.422	0.481	5.710	0.604	5.371	0.538	5.217	0.500	4.961	0.519
Czech Republic	6.743	0.292	8.361	0.483	8.446	0.525	8.366	0.470	8.269	0.484
Denmark	14.803	0.148	19.150	0.216	21.025	0.286	21.420	0.286	21.058	0.268
Estonia	7.523	0.403	8.279	0.492	7.831	0.485	7.320	0.461	6.639	0.466
Finland	12.863	0.212	15.641	0.331	16.885	0.405	17.491	0.427	17.396	0.423
France	11.427	0.236	13.615	0.317	15.177	0.408	16.751	0.422	18.795	0.502
Germany	12.346	0.384	16.799	0.378	18.914	0.453	20.413	0.453	20.317	0.476
Hungary	6.853	0.344	8.090	0.530	7.994	0.564	8.163	0.508	9.180	0.489
Ireland	13.883	0.244	17.645	0.282	21.081	0.375	23.346	0.403	20.595	0.413
Italy	10.145	0.195	13.310	0.328	16.645	0.527	19.619	0.536	20.834	0.585
Latvia	6.239	0.328	6.817	0.455	6.114	0.390	6.057	0.394	5.888	0.403
Netherlands	11.374	0.244	15.759	0.257	17.756	0.340	18.936	0.339	18.436	0.355
Poland	7.009	0.322	8.866	0.500	9.386	0.566	9.173	0.505	9.572	0.570
Portugal	7.378	0.337	9.670	0.531	12.046	0.666	14.659	0.646	13.544	0.623
Romania	5.370	0.500	5.946	0.653	5.949	0.614	6.073	0.612	6.163	0.659
Slovakia	6.664	0.302	8.184	0.527	7.925	0.522	7.787	0.479	7.840	0.502
Slovenia	9.102	0.273	11.396	0.446	12.699	0.520	14.101	0.530	16.464	0.607
Spain	10.639	0.297	12.445	0.382	14.216	0.447	16.578	0.434	18.952	0.441
Sweden	12.005	0.133	14.394	0.235	15.589	0.314	15.752	0.329	15.401	0.301
UK	12.293	0.316	16.982	0.397	17.516	0.467	18.285	0.475	16.471	0.474

Note: Age: 2 – less than 30 years, 3 – from 30 to 39 years, 4 – from 40 to 49 years, 5 – from 50 to 59 years, 6 – 60 years or over; n – no. of observations; mean – average wage in the group; cv – coefficient of variation.

Source: authors' own.

Table 8

Point estimates of correlations (below diagonal in italics) and standard deviations (on the diagonal) of the error terms in case of model  $M_1$ .

	Austria	Belgium	Bulgaria	Czech Republic	Denmark	Estonia	Finland	France	Germany	Hungary	Ireland	Italy	Latvia	Netherlands	Poland	Portugal	Romania	Slovakia	Slovenia	Spain	Sweden	UK		
Austria	0.186																							
Belgium	<i>0.864</i>	0.121																						
Bulgaria	<i>0.628</i>	<i>0.603</i>	0.194																					
Czech Republic	<i>0.858</i>	<i>0.789</i>	<i>0.845</i>	0.195																				
Denmark	<i>0.859</i>	<i>0.822</i>	<i>0.715</i>	<i>0.886</i>	0.120																			
Estonia	<i>0.807</i>	<i>0.734</i>	<i>0.851</i>	<i>0.920</i>	<i>0.848</i>	0.203																		
Finland	<i>0.789</i>	<i>0.880</i>	<i>0.673</i>	<i>0.803</i>	<i>0.908</i>	<i>0.799</i>	0.151																	
France	<i>0.800</i>	<i>0.858</i>	<i>0.564</i>	<i>0.750</i>	<i>0.800</i>	<i>0.692</i>	<i>0.861</i>	0.135																
Germany	<i>0.859</i>	<i>0.755</i>	<i>0.674</i>	<i>0.830</i>	<i>0.910</i>	<i>0.813</i>	<i>0.788</i>	<i>0.749</i>	0.153															
Hungary	<i>0.745</i>	<i>0.697</i>	<i>0.815</i>	<i>0.896</i>	<i>0.831</i>	<i>0.829</i>	<i>0.794</i>	<i>0.729</i>	<i>0.759</i>	0.174														
Ireland	<i>0.597</i>	<i>0.504</i>	<i>0.232</i>	<i>0.495</i>	<i>0.553</i>	<i>0.498</i>	<i>0.451</i>	<i>0.492</i>	<i>0.435</i>	<i>0.405</i>	0.145													
Italy	<i>0.803</i>	<i>0.823</i>	<i>0.434</i>	<i>0.726</i>	<i>0.743</i>	<i>0.594</i>	<i>0.762</i>	<i>0.796</i>	<i>0.591</i>	<i>0.654</i>	<i>0.671</i>	0.193												
Latvia	<i>0.779</i>	<i>0.663</i>	<i>0.833</i>	<i>0.896</i>	<i>0.825</i>	<i>0.916</i>	<i>0.726</i>	<i>0.621</i>	<i>0.783</i>	<i>0.833</i>	<i>0.491</i>	<i>0.556</i>	0.155											
Netherlands	<i>0.781</i>	<i>0.626</i>	<i>0.495</i>	<i>0.765</i>	<i>0.808</i>	<i>0.674</i>	<i>0.677</i>	<i>0.681</i>	<i>0.779</i>	<i>0.689</i>	<i>0.637</i>	<i>0.694</i>	<i>0.694</i>	0.116										
Poland	<i>0.802</i>	<i>0.828</i>	<i>0.723</i>	<i>0.857</i>	<i>0.805</i>	<i>0.833</i>	<i>0.830</i>	<i>0.780</i>	<i>0.685</i>	<i>0.814</i>	<i>0.597</i>	<i>0.775</i>	<i>0.780</i>	<i>0.615</i>	0.193									
Portugal	<i>0.758</i>	<i>0.756</i>	<i>0.522</i>	<i>0.718</i>	<i>0.715</i>	<i>0.632</i>	<i>0.686</i>	<i>0.714</i>	<i>0.593</i>	<i>0.662</i>	<i>0.653</i>	<i>0.832</i>	<i>0.634</i>	<i>0.695</i>	<i>0.731</i>	0.223								
Romania	<i>0.687</i>	<i>0.728</i>	<i>0.867</i>	<i>0.804</i>	<i>0.677</i>	<i>0.774</i>	<i>0.718</i>	<i>0.611</i>	<i>0.627</i>	<i>0.779</i>	<i>0.166</i>	<i>0.562</i>	<i>0.726</i>	<i>0.431</i>	<i>0.755</i>	<i>0.559</i>	0.229							
Slovakia	<i>0.770</i>	<i>0.770</i>	<i>0.875</i>	<i>0.949</i>	<i>0.870</i>	<i>0.886</i>	<i>0.832</i>	<i>0.756</i>	<i>0.804</i>	<i>0.877</i>	<i>0.365</i>	<i>0.654</i>	<i>0.884</i>	<i>0.692</i>	<i>0.817</i>	<i>0.675</i>	<i>0.824</i>	0.202						
Slovenia	<i>0.738</i>	<i>0.847</i>	<i>0.598</i>	<i>0.758</i>	<i>0.708</i>	<i>0.633</i>	<i>0.771</i>	<i>0.826</i>	<i>0.605</i>	<i>0.750</i>	<i>0.404</i>	<i>0.842</i>	<i>0.582</i>	<i>0.562</i>	<i>0.833</i>	<i>0.781</i>	<i>0.708</i>	<i>0.769</i>	0.162					
Spain	<i>0.845</i>	<i>0.835</i>	<i>0.637</i>	<i>0.816</i>	<i>0.795</i>	<i>0.828</i>	<i>0.757</i>	<i>0.759</i>	<i>0.729</i>	<i>0.675</i>	<i>0.608</i>	<i>0.726</i>	<i>0.752</i>	<i>0.667</i>	<i>0.807</i>	<i>0.727</i>	<i>0.688</i>	<i>0.726</i>	<i>0.654</i>	0.160				
Sweden	<i>0.746</i>	<i>0.805</i>	<i>0.656</i>	<i>0.800</i>	<i>0.912</i>	<i>0.743</i>	<i>0.929</i>	<i>0.845</i>	<i>0.822</i>	<i>0.759</i>	<i>0.380</i>	<i>0.709</i>	<i>0.687</i>	<i>0.682</i>	<i>0.715</i>	<i>0.612</i>	<i>0.639</i>	<i>0.819</i>	<i>0.705</i>	<i>0.718</i>	0.123			
UK	<i>0.709</i>	<i>0.613</i>	<i>0.432</i>	<i>0.668</i>	<i>0.726</i>	<i>0.642</i>	<i>0.658</i>	<i>0.657</i>	<i>0.687</i>	<i>0.632</i>	<i>0.693</i>	<i>0.654</i>	<i>0.618</i>	<i>0.806</i>	<i>0.656</i>	<i>0.662</i>	<i>0.370</i>	<i>0.596</i>	<i>0.542</i>	<i>0.656</i>	<i>0.628</i>	0.158		

Note: Estimates obtained on the basis of matrix S of sample variances and covariances of OLS residuals according to the Zellner (1962) method; see formula (4). In the case of model  $M_0$  all of the diagonal elements are zero.

Source: authors' own.